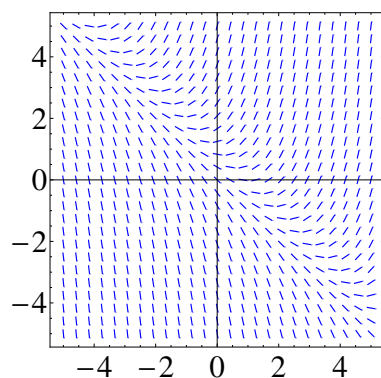


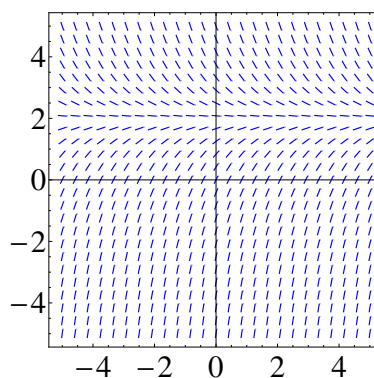
MA 114 Worksheet #28: Direction fields, Separable Differential Equations

1. Match the differential equation with its slope field. Give reasons for your answer.

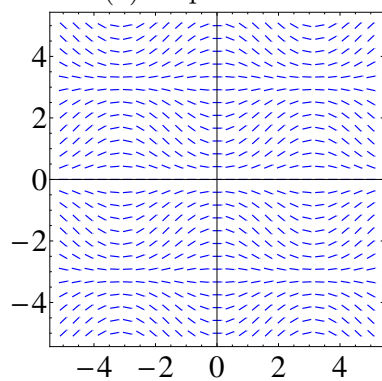
$$y' = 2 - y \quad y' = x(2 - y) \quad y' = x + y - 1 \quad y' = \sin(x) \sin(y)$$



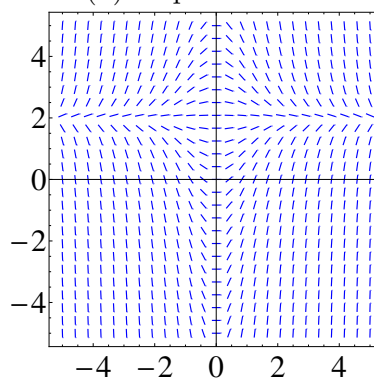
(a) Slope field I



(b) Slope field II



(c) Slope Field III



(d) Slope field IV

Figure 1: Slope fields for Problem 1

2. Use slope field labeled IV to sketch the graphs of the solutions that satisfy the given initial conditions

$$y(0) = -1, \quad y(0) = 0, \quad y(0) = 1.$$

3. Sketch the slope field of the differential equation. Then use it to sketch a solution curve that passes through the given point

(a) $y' = y^2$, $(1, 1)$

(b) $y' = y - 2x$, $(1, 0)$

(c) $y' = xy - x^2$, $(0, 1)$

4. Consider the autonomous differential equation $y' = y^2(3 - y)(y + 1)$. Without solving the differential equation, determine the value of $\lim_{t \rightarrow \infty} y(t)$, where the initial value is
 - (a) $y(0) = 1$
 - (b) $y(0) = 4$
 - (c) $y(0) = -4$
5. Use Euler's method with step size 0.5 to compute the approximate y -values, y_1 , y_2 , y_3 , and y_4 of the solution of the initial-value problem $y' = y - 2x$, $y(1) = 0$.
6. Use separation of variables to find the general solutions to the following differential equations.
 - (a) $y' + 4xy^2 = 0$
 - (b) $\sqrt{1 - x^2}y' = xy$
 - (c) $(1 + x^2)y' = x^3y$
 - (d) $\sqrt{1 + y^2}y' + \sec x = 0$